

Please submit your answers typed up in TeX, either in hard copy or via e-mail by 1 pm on April 24.

1. **(30 points)** Let  $P$  be the poset obtained by removing the  $\hat{0}$  and  $\hat{1}$  elements from  $D_{36}$  (the poset of divisors of 36).
  - (a) Draw a Hasse Diagram of  $P$ .
  - (b) Draw a Hasse Diagram of  $J(P)$ .
  - (c) Draw the order complex  $\Delta(P)$ .
  
2. **(40 points)** Let  $\mathcal{A}$  be the arrangement of 16 hyperplanes  $x_i = 0$  and  $x_i = 1$  for  $i = 1, \dots, 4$ .
  - (a) Compute the characteristic polynomial  $\chi_{\mathcal{A}}(x)$ .
  - (b) Use the characteristic polynomial to compute the number of bounded and unbounded regions of  $\mathcal{A}$ .
  
3. **(30 points)** Let  $\Pi_4$  be the partition lattice, i.e. the poset of partitions of the set  $\{1, 2, 3, 4\}$ . Draw a Hasse diagram of  $\Pi_4$ , and label each element  $x$  with the value of  $\mu_{\Pi_4}(\hat{0}, x)$ , where  $\mu_{\Pi_4}$  is the Möbius function.