

(Problems selected from worksheets by Rob Bayer and from Stewart's *Calculus*)

(1) Integrate each of the following:

(a) $\int e^{x+e^x} dx.$

(b) $\int \frac{\ln(x+1)}{x^2} dx.$

(c) $\int \frac{t^3+1}{t^3-t^2} dt.$

(d) $\int \sqrt{\frac{x-1}{x+1}} dx.$

(e) $\int \frac{dt}{\sqrt{e^t}}.$

(f) $\int \cos^3(2x) \sin(2x) dx$

(2) Find $\frac{dy}{dx}$ using implicit differentiation.

(a) $x^3 + y^3 = 1.$

(b) $x^2 y^2 + x \sin y = 4.$

(c) $2\sqrt{x} + \sqrt{y} = 3.$

(d) $\sin x + \cos y = \sin x \cos y.$

(e) $e^{x/y} = x - y.$

(f) $y \sin(x^2) = x \sin(y^2).$

(3) Find y'' in terms of x and y using implicit differentiation.

(a) $9x^2 + y^2 = 9.$

(b) $y' = x^2 y^2 + 5e^y.$

(c) $\sqrt{x} + \sqrt{y} = 1.$

(d) $y' + xy = x^2.$